

QUIZEN – Vectors and Calculus(11P03)

| Learning Level 1 | Learning Level 2 | Learning Level 3 |
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| Q - Remembering (knowledge-based questions) U - Understanding (comprehension-based questions) | I - Applying (application-based questions) Z - Analyzing (analysis-based questions) | E - Evaluating (evaluation-based questions) N - Creating (creation-based questions) |

Learning Level 1

1. Define the term "vector" and provide an example.
2. State the three operations that can be performed on vectors.
3. What is the magnitude of a vector? How is it calculated?
4. Explain the concept of a dot product between two vectors.
5. Differentiate between a scalar and a vector quantity.

Learning Level 2

6. Given two vectors $A = 3i + 2j$ and $B = 5i - 4j$, calculate the magnitude of the vector sum $A + B$.
7. A particle moves along a curve described by the vector function $r(t) = 2ti + (t^2 - 1)j$. Find the velocity and acceleration vectors of the particle at time $t = 2$.
8. A force $F = (2t + 1)i - (3t - 2)j$ acts on an object. Find the work done by this force as the object moves from the point $(1, -2)$ to $(3, 4)$.
9. Given the vector equation of a line as $r = 2i + 3j + t(4i - 2j)$, determine the direction vector and a point on the line.

10. The position vector of a particle moving in space is given by $r(t) = (2t^2)i + (3t - 1)j + (t^3 - 4t)k$. Calculate the velocity and acceleration vectors of the particle at time $t = 1$.

Learning Level 3

11. A particle moves along a curve described by the vector function $r(t) = (t^2)i + (2t)j$. Find the unit tangent vector and the unit normal vector at time $t = 3$.

12. A vector field is given by $F = (2x + 3y)i + (4y^2 - 2x)j$. Find the curl and divergence of the vector field.

13. Consider the scalar function $f(x, y) = 2x^2 + 3xy - 4y^2$. Determine the critical points and classify them as local maximum, local minimum, or saddle points.

14. Find the directional derivative of the scalar function $f(x, y, z) = 3x^2 + yz$ at the point $(1, -2, 3)$ in the direction of the vector $v = 2i - 3j + 6k$.

15. A particle moves along a curve described by the vector function $r(t) = (t^2)i + (2t)j + (3t^3 - 4t^2)k$. Find the curvature of the curve at time $t = 1$.